JEE MAIN 2015

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Subjects: JEE Main 2015 CBT Exam EH

Q.1 A particle is moving in a circle of radius r under the action of a force $F=\alpha r^2$ which is directed towards centre of the circle. Total mechanical energy (kinetic energy + potential energy) of the particle is (take potential energy = 0 for r = 0) :

Chosen Answer : --

Options

1. $\frac{4}{3}\alpha r^3$
2. $\frac{5}{6}\alpha r^3$
3. αr^3
4. $\frac{1}{2}\alpha r^3$

Q.2 A beaker contains a fluid of density ρ kg/m^3, specific heat S J/kg°C and viscosity η. The beaker is filled up to height h. To estimate the rate of heat transfer per unit area $(\dot{Q}/A)$ by convection when beaker is put on a hot plate, a student proposes that it should depend on η, $\left(\frac{S\Delta\theta}{h}\right)$ and $\left(\frac{1}{\rho g}\right)$ when $\Delta\theta$ (in °C) is the difference in the temperature between the bottom and top of the fluid. In that situation the correct option for $(\dot{Q}/A)$ is :

Chosen Option : 3

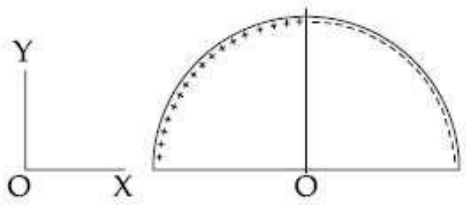
Options

1. $\eta\left(\frac{S\Delta\theta}{h}\right)\left(\frac{1}{\rho g}\right)$
2. $\eta\frac{S\Delta\theta}{h}$
3. $\left(\frac{S\Delta\theta}{\eta h}\right)\left(\frac{1}{\rho g}\right)$

4. $\frac{S\Delta\theta}{\eta h}$

Q.3 A wire, of length L(=20 cm), is bent into a semi-circular arc. If the two equal halves, of the arc, were each to be uniformly charged with charges $\pm Q$, [$|Q| = 10^3\ \varepsilon_0$ Coulomb where ε_0 is the permittivity (in SI units) of free space] the net electric field at the centre O of the semi-circular arc would be :

Chosen Answer : --



Options

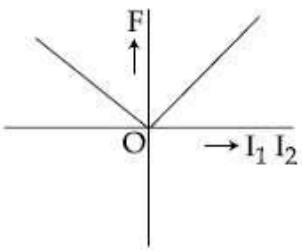
1. $(50\times10^3\ \text{N/C})\ \hat{j}$
2. $(25\times10^3\ \text{N/C})\ \hat{j}$
3. $(50\times10^3\ \text{N/C})\ \hat{i}$
4. $(25\times10^3\ \text{N/C})\ \hat{i}$

Q.4 Two long straight parallel wires, carrying (adjustable) currents I_1 and I_2, are kept at a distance d apart. If the force 'F' between the two wires is taken as 'positive' when the wires repel each other and 'negative' when the wires attract each other, the graph showing the dependence of 'F', on the product I_1I_2, would be :

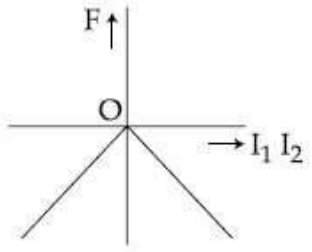
Chosen Answer : --

Options

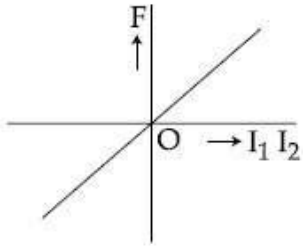
1.



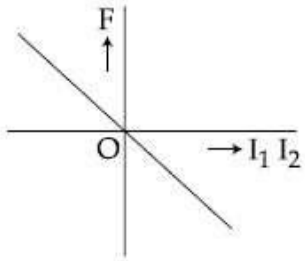
2.



3.

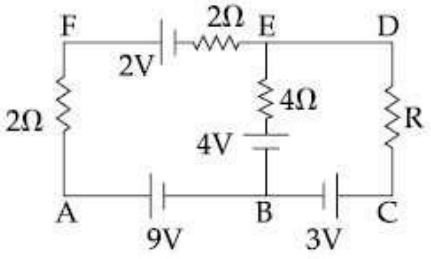


4.



Q.5 In the electric network shown, when no current flows through the 4 Ω resistor in the arm EB, the potential difference between the points A and D will be :

Chosen Answer : --



Options

1. 5 V
2. 6 V
3. 4 V
4. 3 V

Q.6

Chosen Answer : --

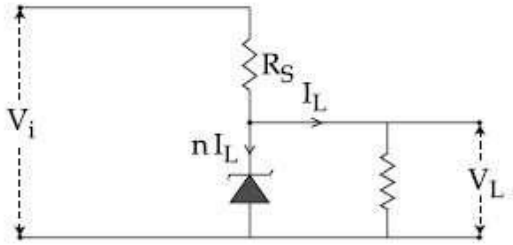
Using equipartition of energy, the specific heat (in J $kg^{-1} K^{-1}$) of aluminium at room temperature can be estimated to be (atomic weight of aluminium = 27)

Options

1. 925
2. 1850
3. 25
4. 410

Q.7 The value of the resistor, R_S, needed in the dc voltage regulator circuit shown here, equals :

Chosen Answer : --

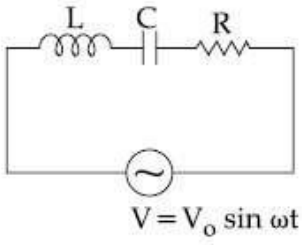


Options

1. $(V_i - V_L)/(n+1)\ I_L$
2. $(V_i + V_L)/n\ I_L$
3. $(V_i + V_L)/(n+1)\ I_L$
4. $(V_i - V_L)/n\ I_L$

Q.8 For the LCR circuit, shown here, the current is observed to lead the applied voltage. An additional capacitor C', when joined with the capacitor C present in the circuit, makes the power factor of the circuit unity. The capacitor C', must have been connected in :

Chosen Answer : --



Options

1. series with C and has a magnitude $\frac{1 - \omega^2 LC}{\omega^2 L}$.
2. series with C and has a magnitude $\frac{C}{(\omega^2 LC - 1)}$.

parallel with C and has a magnitude $\frac{1-\omega^2 LC}{\omega^2 L}$.

3.

parallel with C and has a magnitude $\frac{C}{(\omega^2 LC-1)}$.

4.

Q.9

An electric field $\vec{E} = \left(25\,\hat{i} + 30\,\hat{j}\right) NC^{-1}$ exists in a region of space. If the potential at the origin is taken to be zero then the potential at $x=2$ m, $y=2$ m is :

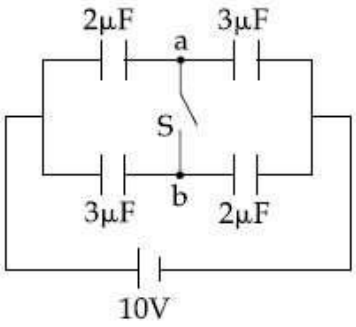
Chosen Option : **3**

Options

1. -120 J
2. -130 J
3. -110 J
4. -140 J

Q.10

In figure is shown a system of four capacitors connected across a 10 V battery. Charge that will flow from switch S when it is closed is :



Chosen Answer : **--**

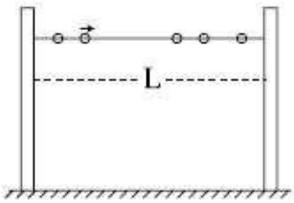
Options

1. 5 μC from a to b
2. zero
3. 5 μC from b to a
4. 20 μC from a to b

Q.11

Chosen Answer : **--**

A large number (n) of identical beads, each of mass m and radius r are strung on a thin smooth rigid horizontal rod of length L (L>>r) and are at rest at random positions. The rod is mounted between two rigid supports (see figure). If one of the beads is now given a speed v, the average force experienced by each support after a long time is (assume all collisions are elastic) :



Options

1. $\frac{mv^2}{L - nr}$
2. $\frac{mv^2}{2(L - nr)}$
3. $\frac{mv^2}{L - 2nr}$
4. zero

Q.12

A particle of mass 2 kg is on a smooth horizontal table and moves in a circular path of radius 0.6 m. The height of the table from the ground is 0.8 m. If the angular speed of the particle is 12 rad s^{-1}, the magnitude of its angular momentum about a point on the ground right under the centre of the circle is :

Chosen Option : **3**

Options

1. 20.16 kg m^2s^{-1}
2. 11.52 kg m^2s^{-1}
3. 8.64 kg m^2s^{-1}
4. 14.4 kg m^2s^{-1}

Q.13

Chosen Answer : **--**

A cylindrical block of wood (density = 650 kg m^{-3}), of base area 30 cm^2 and height 54 cm, floats in a liquid of density 900 kg m^{-3}. The block is depressed slightly and then released. The time period of the resulting oscillations of the block would be equal to that of a simple pendulum of length (nearly) :

Options

1. 39 cm
2. 65 cm
3. 26 cm
4. 52 cm

Q.14 The de - Broglie wavelength associated with the electron in the n = 4 level is :

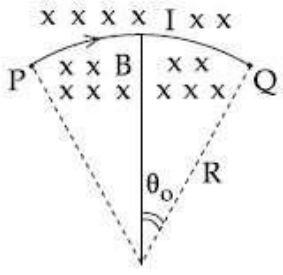
Chosen Option : 3

Options

1. two times the de-Broglie wavelength of the electron in the ground state
2. half of the de-Broglie wavelength of the electron in the ground state
3. four times the de-Broglie wavelength of the electron in the ground state
4. $1/4^{th}$ of the de-Broglie wavelength of the electron in the ground state

Q.15 A wire carrying current I is tied between points P and Q and is in the shape of a circular arch of radius R due to a uniform magnetic field B (perpendicular to the plane of the paper, shown by xxx) in the vicinity of the wire. If the wire subtends an angle $2\theta_0$ at the centre of the circle (of which it forms an arch) then the tension in the wire is :

Chosen Option : 3



Options

1. IBR

2. $\frac{IBR\theta_0}{\sin\theta_0}$

3. $\frac{IBR}{\sin\theta_0}$

4. $\frac{IBR}{2\sin\theta_0}$

Q.16 Unpolarized light of intensity I_0 is incident on surface of a block of glass at Brewster's angle. In that case, which one of the following statements is true ?

Chosen Answer : **--**

Options

1. reflected light is partially polarized with intensity $I_0/2$.

2. reflected light is completely polarized with intensity less than $I_0/2$.

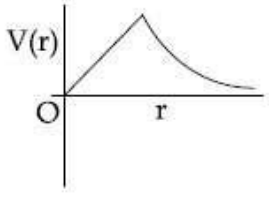
3. transmitted light is partially polarized with intensity $I_0/2$.

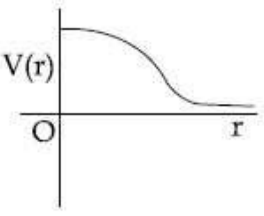
4. transmitted light is completely polarized with intensity less than $I_0/2$.

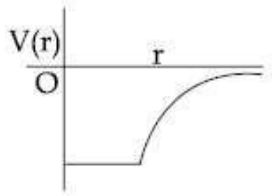
Q.17 Which of the following most closely depicts the correct variation of the gravitation potential V(r) due to a large planet of radius R and uniform mass density ? *(figures are not drawn to scale)*

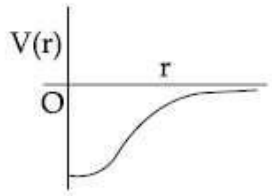
Chosen Option : **3**

Options

1. 

2. 

3. 

4. 

Q.18 A short bar magnet is placed in the magnetic meridian of the earth with north pole pointing north. Neutral points are found at a distance of 30 cm from the magnet on the East - West line, drawn through the middle point of the magnet. The magnetic moment of the magnet in Am^2 is close to :

(Given $\frac{\mu_0}{4\pi} = 10^{-7}$ in SI units and B_H = Horizontal component of earth's magnetic field = 3.6×10^{-5} Tesla.)

Chosen Answer : --

Options

1. 4.9
2. 14.6
3. 9.7
4. 19.4

Q.19 The AC voltage across a resistance can be measured using a :

Chosen Option : **4**

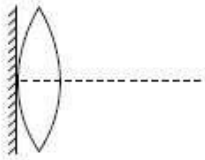
Options

1. hot wire voltmeter
2. moving magnet galvanometer
3. moving coil galvanometer
4. potentiometer

Q.20

Chosen Option : **2**

A thin convex lens of focal length 'f' is put on a plane mirror as shown in the figure. When an object is kept at a distance 'a' from the lens - mirror combination, its image is formed at a distance $\frac{a}{3}$ in front of the combination. The value of 'a' is :



Options
1. $2f$
2. $\frac{3}{2}f$
3. $3f$
4. f

Q.21

In a Young's double slit experiment with light of wavelength λ the separation of slits is d and distance of screen is D such that $D >> d >> \lambda$. If the Fringe width is β, the distance from point of maximum intensity to the point where intensity falls to half of maximum intensity on either side is :

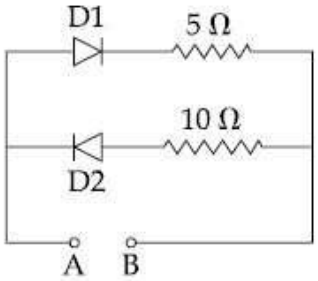
Chosen Answer : --

Options
1. $\frac{\beta}{2}$
2. $\frac{\beta}{6}$
3. $\frac{\beta}{4}$
4. $\frac{\beta}{3}$

Q.22

Chosen Option : 1

A 2V battery is connected across AB as shown in the figure. The value of the current supplied by the battery when in one case battery's positive terminal is connected to A and in other case when positive terminal of battery is connected to B will respectively be :



Options
1. 0.4 A and 0.2 A
2. 0.2 A and 0.1 A
3. 0.1 A and 0.2 A
4. 0.2 A and 0.4 A

Q.23 A uniform thin rod AB of length L has linear mass density $\mu(x) = a + \frac{bx}{L}$, where x is measured from A. If the CM of the rod lies at a distance of $\left(\frac{7}{12}L\right)$ from A, then a and b are related as :

Chosen Answer : --

Options
1. $3a = 2b$
2. $a = b$
3. $2a = b$
4. $a = 2b$

Q.24 A vector $\vec{A}$ is rotated by a small angle $\Delta\theta$ radians ($\Delta\theta << 1$) to get a new vector $\vec{B}$. In that case $|\vec{B} - \vec{A}|$ is :

Chosen Option : 3

Options
1. $|\vec{A}|\,\Delta\theta$
2. $|\vec{A}|\left(1 - \frac{\Delta\theta^2}{2}\right)$
3. 0

4. $|\vec{B}|\,\Delta\theta - |\vec{A}|$

Q.25 If electronic charge e, electron mass m, speed of light in vacuum c and Planck's constant h are taken as fundamental quantities, the permeability of vacuum μ_0 can be expressed in units of :

Chosen Answer : --

Options

1. $\left(\frac{h}{ce^2}\right)$
2. $\left(\frac{mc^2}{he^2}\right)$
3. $\left(\frac{h}{me^2}\right)$
4. $\left(\frac{hc}{me^2}\right)$

Q.26 Let N_β be the number of β particles emitted by 1 gram of Na^{24} radioactive nuclei (half life = 15 hrs) in 7.5 hours, N_β is close to (Avogadro number $= 6.023 \times 10^{23}$/g. mole) :

Chosen Answer : --

Options

1. 7.5×10^{21}
2. 6.2×10^{21}
3. 1.25×10^{22}
4. 1.75×10^{22}

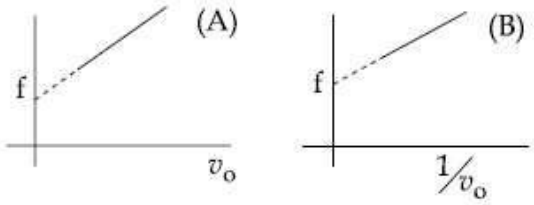
Q.27 An experiment takes 10 minutes to raise the temperature of water in a container from 0°C to 100°C and another 55 minutes to convert it totally into steam by a heater supplying heat at a uniform rate. Neglecting the specific heat of the container and taking specific heat of water to be 1 cal/g °C, the heat of vapourization according to this experiment will come out to be :

Chosen Answer : --

Options

1. 550 cal/g
2. 560 cal/g
3. 540 cal/g
4. 530 cal/g

Q.28 A source of sound emits sound waves at frequency f_0. It is moving towards an observer with fixed speed v_s(v_s<v, where v is the speed of sound in air). If the observer were to move towards the source with speed v_0, one of the following two graphs (A and B) will give the correct variation of the frequency f heard by the observer as v_0 is changed.



The variation of f with v_0 is given correctly by :

Chosen Option : **3**

Options

1. graph A with slope $= \frac{f_0}{(v + v_s)}$

2. graph B with slope $= \frac{f_0}{(v + v_s)}$

3. graph A with slope $= \frac{f_0}{(v - v_s)}$

4. graph B with slope $= \frac{f_0}{(v - v_s)}$

Q.29 A pendulum with time period of 1s is losing energy due to damping. At certain time its energy is 45 J. If after completing 15 oscillations, its energy has become 15 J, its damping constant (in s^{-1}) is :

Chosen Answer : **--**

Optio

ns

1. $\frac{1}{2}$
2. 2
3. $\frac{1}{15}ln\,3$
4. $\frac{1}{30}ln\,3$

Q.30 For plane electromagnetic waves propagating in the z direction, which one of the following combination gives the correct possible direction for $\vec{E}$ and $\vec{B}$ field respectively ?

Chosen Option : 1

Options

1. $\left(3\hat{i}+4\hat{j}\right)$ and $\left(4\hat{i}-3\hat{j}\right)$
2. $\left(-2\hat{i}-3\hat{j}\right)$ and $\left(3\hat{i}-2\hat{j}\right)$
3. $\left(\hat{i}+2\hat{j}\right)$ and $\left(2\hat{i}-\hat{j}\right)$
4. $\left(2\hat{i}+3\hat{j}\right)$ and $\left(\hat{i}+2\hat{j}\right)$

Q.1 Chlorine water on standing loses its colour and forms :

Chosen Option : 1

Options

1. HCl and $HOCl$
2. HCl only
3. $HOCl$ and $HOCl_2$
4. HCl and $HClO_2$

Q.2 The increase of pressure on ice $\rightleftharpoons$ water system at constant temperature will lead to :

Chosen Option : 2

Options

1. a shift of the equilibrium in the forward direction
2. an increase in the Gibbs energy of the system
3. a decrease in the entropy of the system
4. no effect on the equilibrium

Q.3 Which of the alkaline earth metal halides given below is essentially covalent in nature ?

Chosen Option : 3

Options
1. $CaCl_2$
2. $BeCl_2$
3. $SrCl_2$
4. $MgCl_2$

Q.4 Addition of phosphate fertilisers to water bodies causes :

Chosen Answer : --

Options
1. enhanced growth of algae
2. increase in amount of dissolved oxygen in water
3. increase in fish population
4. deposition of calcium phosphate

Q.5 Which of the following compounds has a P – P bond ?

Chosen Option : 4

Options
1. $H_4P_2O_7$
2. $H_4P_2O_5$
3. $(HPO_3)_3$
4. $H_4P_2O_6$

Q.6 Accumulation of which of the following molecules in the muscles occurs as a result of vigorous exercise ?

Chosen Option : 1

Options
1. Glycogen
2. L-lactic acid
3. Pyruvic acid
4. Glucose

Q.7 In the reaction sequence

$2\,CH_3CHO \xrightarrow{OH^-} A \xrightarrow{\Delta} B$; the product B is :

Chosen Option : 2

Options
1. $CH_3-CH_2-CH_2-CH_2-OH$
2. $CH_3-CH=CH-CHO$
3. $CH_3-\overset{\overset{O}{\|}}{C}-CH_3$

4. $CH_3-CH_2-CH_2-CH_3$

Q.8 For the equilibrium, $A(g) \rightleftharpoons B(g)$, ΔH is -40 kJ/mol. If the ratio of the activation energies of the forward (E_f) and reverse (E_b) reactions is $\frac{2}{3}$ then :

Chosen Answer : --

Options
1. $E_f = 30$ kJ/mol ; $E_b = 70$ kJ/mol
2. $E_f = 80$ kJ/mol ; $E_b = 120$ kJ/mol
3. $E_f = 60$ kJ/mol ; $E_b = 100$ kJ/mol
4. $E_f = 70$ kJ/mol ; $E_b = 30$ kJ/mol

Q.9 Match the organic compounds in **column - I** with the Lassaigne's test results in **column - II** appropriately :

Chosen Answer : --

Column - I		Column - II	
(A)	Aniline	(i)	Red color with $FeCl_3$
(B)	Benzene sulfonic acid	(ii)	Violet color with sodium nitroprusside
(C)	Thiourea	(iii)	Blue color with hot and acidic solution of $FeSO_4$

Options
1. (A) - (iii) ; (B) - (ii) ; (C) - (i)
2. (A) - (ii) ; (B) - (i) ; (C) - (iii)
3. (A) - (iii) ; (B) - (i) ; (C) - (ii)
4. (A) - (ii) ; (B) - (iii) ; (C) - (i)

Q.10 Which of the following complex ions has electrons that are symmetrically filled in both t_{2g} and e_g orbitals ?

Chosen Answer : --

Options
1. $[FeF_6]^{3-}$

2. $[Mn(CN)_6]^{4-}$

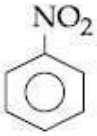
3. $[Co(NH_3)_6]^{2+}$

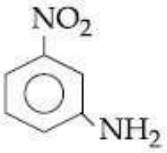
4. $[CoF_6]^{3-}$

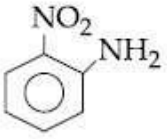
Q.11 Which compound exhibits maximum dipole moment among the following ?

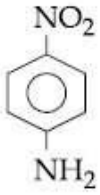
Chosen Option : **4**

Options

1. 

2. 

3. 

4. 

Q.12 Which physical property of dihydrogen is wrong ?

Chosen Option : **2**

Options

1. Tasteless gas
2. Non-inflammable gas
3. Odourless gas
4. Colourless gas

Q.13 A pink coloured salt turns blue on heating. The presence of which cation is most likely ?

Chosen Option : **4**

Options

1. Zn^{2+}
2. Fe^{2+}
3. Cu^{2+}
4. Co^{2+}

Q.14

Chosen Option : **2**

$A + 2B \rightarrow C$, the rate equation for this reaction is given as

$$\text{Rate} = k[A][B].$$

If the concentration of A is kept the same but that of B is doubled what will happen to the rate itself ?

Options
1. halved
2. quadrupled
3. doubled
4. the same

Q.15 Determination of the molar mass of acetic acid in benzene using freezing point depression is affected by :

Chosen Option : **2**

Options
1. partial ionization
2. dissociation
3. complex formation
4. association

Q.16 Which artificial sweetener contains chlorine ?

Chosen Answer : **--**

Options
1. Sucralose
2. Aspartame
3. Alitame
4. Saccharin

Q.17 When concentrated HCl is added to an aqueous solution of $CoCl_2$, its colour changes from reddish pink to deep blue. Which complex ion gives blue colour in this reaction ?

Chosen Option : **4**

Options
1. $[Co(H_2O)_6]^{2+}$
2. $[CoCl_6]^{3-}$
3. $[CoCl_4]^{2-}$
4. $[CoCl_6]^{4-}$

Q.18 At temperature T, the average kinetic energy of any particle is $\frac{3}{2}$ kT. The de Broglie wavelength follows the order :

Chosen Answer : **--**

Options

1. Visible photon > Thermal neutron > Thermal electron

2. Visible photon > Thermal electron > Thermal neutron

3. Thermal proton > Thermal electron > Visible photon

4. Thermal proton > Visible photon > Thermal electron

Q.19 Which of the following statements is false ?

Chosen Option : **2**

Options

1. CrO_4^{2-} is tetrahedral in shape

2. $Na_2Cr_2O_7$ is less soluble than $K_2Cr_2O_7$

3. $Cr_2O_7^{2-}$ has a Cr−O−Cr bond

4. $Na_2Cr_2O_7$ is a primary standard in volumetry

Q.20 When does a gas deviate the most from its ideal behaviour ?

Chosen Option : **1**

Options

1. At high pressure and low temperature

2. At low pressure and low temperature

3. At low pressure and high temperature

4. At high pressure and high temperature

Q.21 Which of the following pairs of compounds are positional isomers ?

Chosen Option : **4**

Options

1. $CH_3-CH_2-CH_2-\underset{\underset{O}{\|}}{C}-CH_3$ and $CH_3-\underset{\underset{CH_3}{|}}{CH}-CH_2-CHO$

2. $CH_3-CH_2-CH_2-CH_2-CHO$ and $CH_3-CH_2-CH_2-\overset{\overset{O}{\|}}{C}-CH_3$

$CH_3-CH_2-\overset{\overset{O}{\|}}{C}-CH_2-CH_3$ and

3. 

$CH_3-CH_2-CH_2-\overset{\overset{O}{\|}}{C}-CH_3$ and

4. $CH_3-CH_2-\overset{\overset{O}{\|}}{C}-CH_2-CH_3$

Q.22 Choose the incorrect formula out of the four compounds for an element X below :

Chosen Option : **3**

Options

1. $X_2(SO_4)_3$
2. X_2O_3
3. X_2Cl_3
4. XPO_4

Q.23 The number of structural isomers for C_6H_{14} is :

Chosen Option : **4**

Options

1. 3
2. 4
3. 6
4. 5

Q.24 At 298 K, the standard reduction potentials are 1.51 V for $MnO_4^- | Mn^{2+}$, 1.36 V for $Cl_2 | Cl^-$, 1.07 V for $Br_2 | Br^-$, and 0.54 V for $I_2 | I^-$. At pH = 3, permanganate is expected to oxidize : $\left(\frac{RT}{F} = 0.059\,V\right)$

Chosen Answer : **--**

Options

1. Cl^-, Br^- and I^-
2. Cl^- and Br^-
3. I^- only

4. Br^- and I^-

Q.25 Under ambient conditions, which among the following surfactants will form micelles in aqueous solution at lowest molar concentration ?

Chosen Option : **3**

Options

1. $CH_3(CH_2)_{15}\overset{\oplus}{N}(CH_3)_3\overset{\ominus}{Br}$

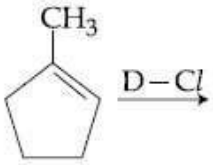
2. $CH_3(CH_2)_{11}\overset{\oplus}{N}(CH_3)_3Br^-$

3. $CH_3-(CH_2)_{13}-OSO_3^-Na^+$

4. $CH_3-(CH_2)_8-\overset{\ominus}{COO}Na^+$

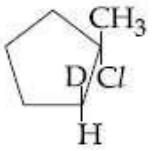
Q.26 What is the major product expected from the following reaction ?

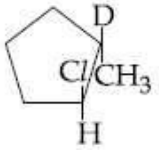
Chosen Answer : **--**

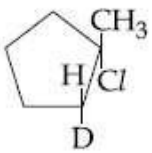


Where D is an isotope of Hydrogen.

Options

1. 

2. 

3. 

4. 

Q.27 Molecule AB has a bond length of 1.617Å and a dipole moment of 0.38 D. The fractional charge on each atom (absolute magnitude) is : ($e_0 = 4.802 \times 10^{-10}$ esu)

Chosen Option : 1

Options
1. 1.0
2. 0.05
3. 0
4. 0.5

Q.28 $A + 2B + 3C \rightleftharpoons AB_2C_3$

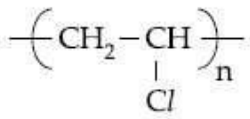
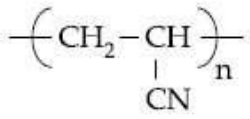
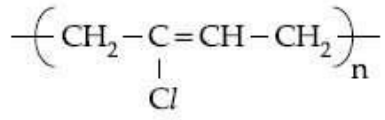
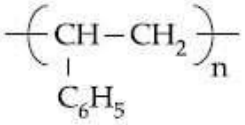
Reaction of 6.0 g of A, 6.0×10^{23} atoms of B, and 0.036 mol of C yields 4.8 g of compound AB_2C_3. If the atomic mass of A and C are 60 and 80 amu, respectively, the atomic mass of B is (Avogadro no. $= 6 \times 10^{23}$) :

Chosen Answer : --

Options
1. 50 amu
2. 60 amu
3. 70 amu
4. 40 amu

Q.29 Which one of the following structures represents the neoprene polymer ?

Chosen Option : 2

Options
1. 
2. 
3. 
4. 

Q.30 Calamine is an ore of :

Chosen Option : 1

Options
1. Iron
2. Zinc
3. Aluminium

4. Copper

Q.1 The term independent of x in the binomial expansion of

$$\left(1-\frac{1}{x}+3x^5\right)\left(2x^2-\frac{1}{x}\right)^8 \text{ is :}$$

Chosen Answer : --

Options
1. 496
2. -496
3. 400
4. -400

Q.2 Let PQ be a double ordinate of the parabola, $y^2=-4x$, where P lies in the second quadrant. If R divides PQ in the ratio 2 : 1, then the locus of R is :

Chosen Answer : --

Options
1. $9y^2=-4x$
2. $3y^2=-2x$
3. $3y^2=2x$
4. $9y^2=4x$

Q.3 If a circle passing through the point $(-1, 0)$ touches y-axis at $(0, 2)$, then the length of the chord of the circle along the x-axis is :

Chosen Answer : --

Options
1. 3
2. $\frac{3}{2}$
3. $\frac{5}{2}$
4. 5

Q.4 If the two roots of the equation, $(a-1)(x^4+x^2+1)+(a+1)(x^2+x+1)^2=0$ are real and distinct, then the set of all values of 'a' is :

Chosen Answer : --

Options
1. $\left(0, \frac{1}{2}\right)$
2. $\left(-\frac{1}{2}, 0\right)\cup\left(0, \frac{1}{2}\right)$

3. $\left(-\frac{1}{2}, 0\right)$

4. $(-\infty, -2) \cup (2, \infty)$

Q.5 In a parallelogram ABCD, $|\overrightarrow{AB}| = a$, $|\overrightarrow{AD}| = b$ and $|\overrightarrow{AC}| = c$, then $\overrightarrow{DB} \cdot \overrightarrow{AB}$ has the value :

Chosen Answer : --

Options

1. $\frac{1}{4}\left(a^2 + b^2 - c^2\right)$

2. $\frac{1}{2}\left(a^2 + b^2 + c^2\right)$

3. $\frac{1}{3}\left(b^2 + c^2 - a^2\right)$

4. $\frac{1}{2}\left(a^2 - b^2 + c^2\right)$

Q.6 Let $A = \{x_1, x_2, ..., x_7\}$ and $B = \{y_1, y_2, y_3\}$ be two sets containing seven and three distinct elements respectively. Then the total number of functions $f : A \to B$ that are onto, if there exist exactly three elements x in A such that $f(x) = y_2$, is equal to :

Chosen Answer : --

Options

1. $14 \cdot {}^7C_3$

2. $14 \cdot {}^7C_2$

3. $12 \cdot {}^7C_2$

4. $16 \cdot {}^7C_3$

Q.7 Let k be a non-zero real number. If

$$f(x) = \begin{cases} \dfrac{(e^x - 1)^2}{\sin\left(\frac{x}{k}\right)\log\left(1 + \frac{x}{4}\right)}, & x \neq 0 \\ 12, & x = 0 \end{cases}$$

is a continuous function, then the value of k is :

Chosen Answer : --

Options

1. 3

2. 1

3. 4

4. 2

Q.8

Chosen Option : **1**

If $\sum_{n=1}^{5} \frac{1}{n(n+1)(n+2)(n+3)} = \frac{k}{3}$, then k is equal to :

Options

1. $\frac{55}{336}$
2. $\frac{19}{112}$
3. $\frac{17}{105}$
4. $\frac{1}{6}$

Q.9 If z is a non-real complex number, then the minimum value of $\frac{\text{Im } z^5}{(\text{Im } z)^5}$ is :

Chosen Answer : --

Options

1. -4
2. -5
3. -1
4. -2

Q.10 A straight line L through the point $(3, -2)$ is inclined at an angle of $60°$ to the line $\sqrt{3}x + y = 1$. If L also intersects the x-axis, then the equation of L is :

Chosen Answer : --

Options

1. $\sqrt{3}y - x + 3 + 2\sqrt{3} = 0$
2. $\sqrt{3}y + x - 3 + 2\sqrt{3} = 0$
3. $y + \sqrt{3}x + 2 - 3\sqrt{3} = 0$
4. $y - \sqrt{3}x + 2 + 3\sqrt{3} = 0$

Q.11 Let $f : (-1, 1) \to \mathbf{R}$ be a continuous function. If $\int_0^{\sin x} f(t)\,dt = \frac{\sqrt{3}}{2}x$, then $f\left(\frac{\sqrt{3}}{2}\right)$ is equal to :

Chosen Answer : --

Options

1. $\frac{\sqrt{3}}{2}$

2. $\sqrt{\frac{3}{2}}$

3. $\frac{1}{2}$

4. $\sqrt{3}$

Q.12 Let 10 vertical poles standing at equal distances on a straight line, subtend the same angle of elevation α at a point O on this line and all the poles are on the same side of O. If the height of the longest pole is 'h' and the distance of the foot of the smallest pole from O is 'a' ; then the distance between two consecutive poles, is :

Chosen Answer : --

Options

1. $\frac{h\cos\alpha - a\sin\alpha}{9\sin\alpha}$

2. $\frac{h\sin\alpha + a\cos\alpha}{9\sin\alpha}$

3. $\frac{h\sin\alpha + a\cos\alpha}{9\cos\alpha}$

4. $\frac{h\cos\alpha - a\sin\alpha}{9\cos\alpha}$

Q.13 The shortest distance between the z-axis and the line $x+y+2z-3=0=2x+3y+4z-4$, is :

Chosen Answer : --

Options

1. 2

2. 1

3. 3

4. 4

Q.14 If the mean and the variance of a binomial variate X are 2 and 1 respectively, then the probability that X takes a value greater than or equal to one is :

Chosen Answer : --

Options

1. $\frac{1}{16}$

2. $\frac{3}{4}$

3. $\frac{15}{16}$

4. $\frac{9}{16}$

Q.15 The sum of the 3rd and the 4th terms of a G.P. is 60 and the product of its first three terms is 1000. If the first term of this G.P. is positive, then its 7th term is :

Chosen Option : 1

Options
1. 2430
2. 320
3. 640
4. 7290

Q.16 Let k and K be the minimum and the maximum values of the function $f(x) = \frac{(1+x)^{0.6}}{1+x^{0.6}}$ in [0, 1] respectively, then the ordered pair (k, K) is equal to :

Chosen Answer : --

Options
1. $(1, 2^{0.6})$
2. $(2^{-0.4}, 1)$
3. $(2^{-0.6}, 1)$
4. $(2^{-0.4}, 2^{0.6})$

Q.17 If $\cos\alpha + \cos\beta = \frac{3}{2}$ and $\sin\alpha + \sin\beta = \frac{1}{2}$ and θ is the arithmetic mean of α and β, then $\sin2\theta + \cos2\theta$ is equal to :

Chosen Answer : --

Options
1. $\frac{8}{5}$
2. $\frac{4}{5}$
3. $\frac{3}{5}$
4. $\frac{7}{5}$

Q.18 If the lengths of the sides of a triangle are decided by the three throws of a single fair die, then the probability that the triangle is of maximum area given that it is an isosceles triangle, is :

Chosen Answer : --

Options
1. $\frac{1}{27}$
2. $\frac{1}{26}$
3. $\frac{1}{21}$

4. $\frac{1}{15}$

Q.19 If the distance between the foci of an ellipse is half the length of its latus rectum, then the eccentricity of the ellipse is :

Chosen Answer : --

Options

1. $\frac{2\sqrt{2}-1}{2}$
2. $\frac{1}{2}$
3. $\sqrt{2}-1$
4. $\frac{\sqrt{2}-1}{2}$

Q.20 If the incentre of an equilateral triangle is (1, 1) and the equation of its one side is $3x+4y+3=0$, then the equation of the circumcircle of this triangle is :

Chosen Answer : --

Options

1. $x^2+y^2-2x-2y-14=0$
2. $x^2+y^2-2x-2y-7=0$
3. $x^2+y^2-2x-2y+2=0$
4. $x^2+y^2-2x-2y-2=0$

Q.21 If in a regular polygon the number of diagonals is 54, then the number of sides of this polygon is :

Chosen Answer : --

Options

1. 6
2. 9
3. 10
4. 12

Q.22 If A is a 3×3 matrix such that $|5.\ \text{adjA}|=5$, then $|A|$ is equal to :

Chosen Option : **1**

Options

1. $\pm\frac{1}{5}$
2. ±1
3. ±5
4. $\pm\frac{1}{25}$

Q.23

Chosen Option : **3**

A plane containing the point (3, 2, 0) and the line $\frac{x-1}{1}=\frac{y-2}{5}=\frac{z-3}{4}$ also contains the point :

Options

1. (0, 7, 10)
2. (0, 3, 1)
3. (0, 7, −10)
4. (0, −3, 1)

Q.24 The equation of a normal to the curve, $\sin y = x \sin\left(\frac{\pi}{3}+y\right)$ at $x=0$, is :

Chosen Answer : --

Options

1. $2x-\sqrt{3}\,y=0$
2. $2y+\sqrt{3}\,x=0$
3. $2x+\sqrt{3}\,y=0$
4. $2y-\sqrt{3}\,x=0$

Q.25 The solution of the differential equation $ydx-(x+2y^2)dy=0$ is $x=f(y)$.
If $f(-1)=1$, then $f(1)$ is equal to :

Chosen Answer : --

Options

1. 3
2. 2
3. 1
4. 4

Q.26 Consider the following statements :

P : Suman is brilliant.

Q : Suman is rich.

R : Suman is honest.

The negation of the statement,

"Suman is brilliant and dishonest if and only if Suman is rich" can be equivalently expressed as :

Chosen Option : 4

Options

1. $\sim Q \leftrightarrow \sim P \vee R$
2. $\sim Q \leftrightarrow P \vee \sim R$
3. $\sim Q \leftrightarrow P \wedge \sim R$
4. $\sim Q \leftrightarrow \sim P \wedge R$

Q.27

Let $f : \mathbf{R} \to \mathbf{R}$ be a function such that $f(2-x)=f(2+x)$ and $f(4-x)=f(4+x)$, for all $x \in \mathbf{R}$ and $\int_0^2 f(x)\,dx = 5$. Then the value of $\int_{10}^{50} f(x)\,dx$ is :

Chosen Answer : --

Options
1. 80
2. 125
3. 100
4. 200

Q.28

From the top of a 64 metres high tower, a stone is thrown upwards vertically with the velocity of 48 m/s. The greatest height (in metres) attained by the stone, assuming the value of the gravitational acceleration $g=32\ m/s^2$, is :

Chosen Option : 4

Options
1. 112
2. 88
3. 128
4. 100

Q.29

If $\begin{vmatrix} x^2+x & x+1 & x-2 \\ 2x^2+3x-1 & 3x & 3x-3 \\ x^2+2x+3 & 2x-1 & 2x-1 \end{vmatrix} = ax-12$,

then 'a' is equal to :

Chosen Answer : --

Options
1. -24
2. 24
3. 12
4. -12

Q.30

If $\int \frac{\log\left(t+\sqrt{1+t^2}\right)}{\sqrt{1+t^2}}\,dt = \frac{1}{2}(g(t))^2 + C$,

where C is a constant, then g(2) is equal to :

Chosen Option : 4

Options
1. $\log(2+\sqrt{5})$
2. $2\log(2+\sqrt{5})$

3. $\frac{1}{2}\log(2+\sqrt{5})$
4. $\frac{1}{\sqrt{5}}\log(2+\sqrt{5})$